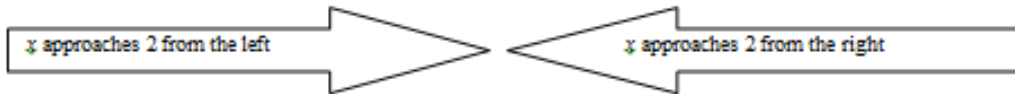




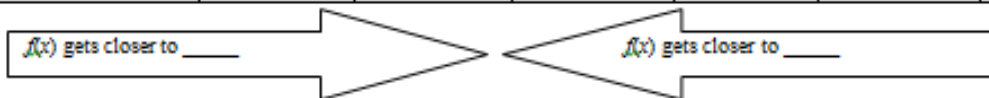
Understanding Limits Numerically and Graphically

In Problems 1-3, complete the table to investigate the limit.

1. $\lim_{x \rightarrow 2} \frac{x^2 - 4}{x - 2}$



x	1.99	1.999	1.9999	2	2.0001	2.001	2.01
$f(x) = \frac{x^2 - 4}{x - 2}$							



The limit of $f(x) = \frac{x^2 - 4}{x - 2}$ as x approaches 2 equals _____.

2. $\lim_{x \rightarrow 3} \frac{1}{x - 2} =$

x	2.99	2.999	2.9999	3	3.0001	3.001	3.01
$f(x) = \frac{1}{x - 2}$							

The limit of $f(x) = \frac{1}{x - 2}$ as x approaches 3 equals _____.

3. $\lim_{x \rightarrow 0} \frac{x}{x^2 + 1}$

x	-0.01	-0.001	-0.0001	0	0.0001	0.001	0.01
$f(x) = \frac{x}{x^2 + 1}$							

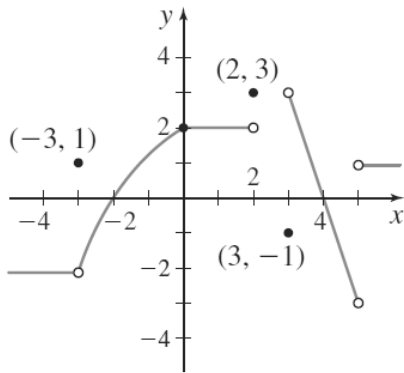
The limit of $f(x) = \frac{x}{x^2 + 1}$ as x approaches 0 equals _____.



Understanding Limits Numerically and Graphically

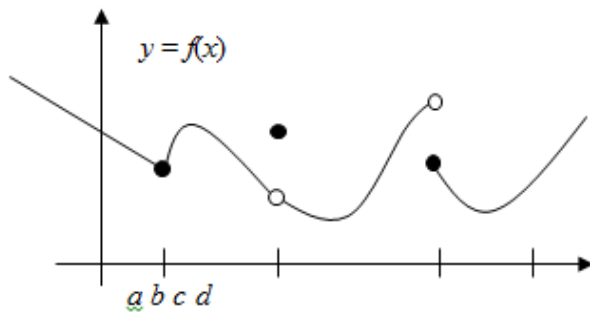
Use the graph of f to find the indicated limit or function value.

- 1. $\lim_{x \rightarrow -4^-} f(x) =$ _____
- 2. $\lim_{x \rightarrow -4^+} f(x) =$ _____
- 3. $\lim_{x \rightarrow -4} f(x) =$ _____
- 4. $f(-4) =$ _____
- 5. $\lim_{x \rightarrow 0} f(x) =$ _____
- 6. $\lim_{x \rightarrow -3} f(x) =$ _____
- 7. $\lim_{x \rightarrow 5^-} f(x) =$ _____
- 8. $\lim_{x \rightarrow -5^+} f(x) =$ _____
- 9. $\lim_{x \rightarrow -5} f(x) =$ _____
- 10. $f(2) =$ _____
- 11. $\lim_{x \rightarrow -2^-} f(x) =$ _____
- 12. $f(-3) =$ _____



For each of the following, determine whether the limit exists on the basis of the graph of $y = f(x)$. The domain of f is the set of real numbers.

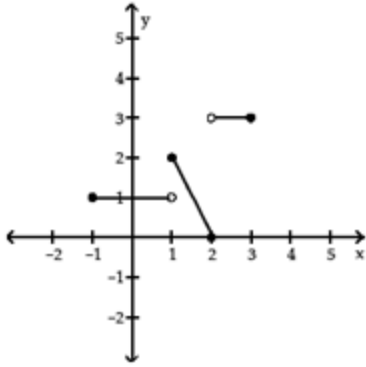
- 13. $\lim_{x \rightarrow a} f(x)$
- 14. $\lim_{x \rightarrow b} f(x)$
- 15. $\lim_{x \rightarrow c} f(x)$
- 16. $\lim_{x \rightarrow c^+} f(x)$
- 17. $\lim_{x \rightarrow c} f(x)$
- 18. $\lim_{x \rightarrow d} f(x)$





Understanding Limits Numerically and Graphically

19. Use the graph to estimate each limit, or state that the limit does not exist.



a. $\lim_{x \rightarrow 1^-} f(x)$

b. $\lim_{x \rightarrow 1^+} f(x)$

c. $\lim_{x \rightarrow 1} f(x)$

d. $\lim_{x \rightarrow 0^-} f(x)$

e. $\lim_{x \rightarrow 0^+} f(x)$

f. $\lim_{x \rightarrow 0} f(x)$



Understanding Limits Numerically and Graphically

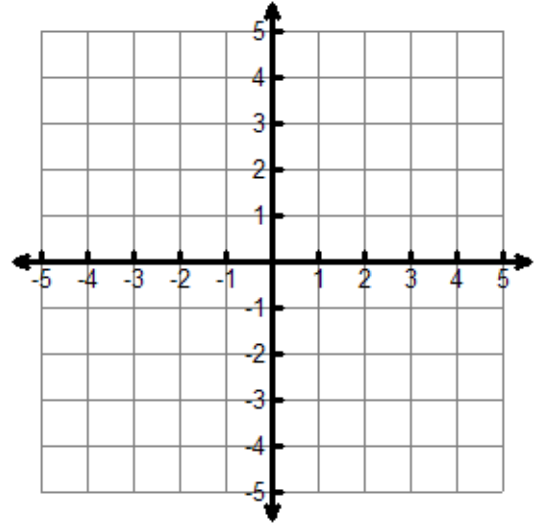
Use the given function to find the indicated limits, or state that the limit does not exist. Verify your answers graphically.

1. $f(x) = \begin{cases} (x+2)^2 & \text{when } x < 0 \\ -\sqrt{x} + 4 & \text{when } x \geq 0 \end{cases}$

a. $\lim_{x \rightarrow 0^-} f(x)$

b. $\lim_{x \rightarrow 0^+} f(x)$

c. $\lim_{x \rightarrow 0} f(x)$

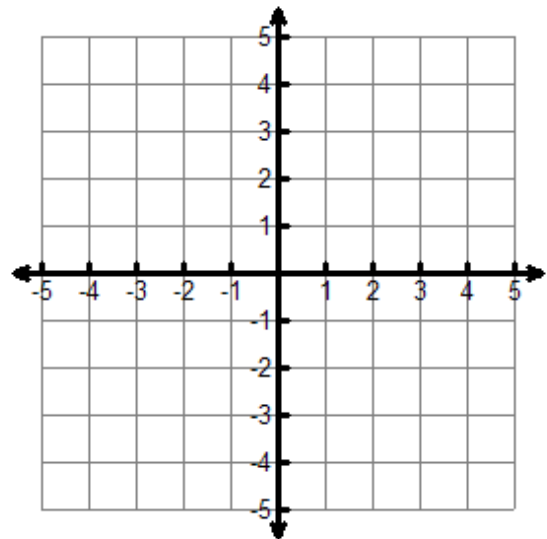


2. $f(x) = \begin{cases} x^2 - 4 & x \leq 2 \\ x - 3 & x > 2 \end{cases}$

a. $\lim_{x \rightarrow 2^-} f(x)$

b. $\lim_{x \rightarrow 2^+} f(x)$

c. $\lim_{x \rightarrow 2} f(x)$





Understanding Limits Numerically and Graphically

$$3. f(x) = \begin{cases} -x & x < 1 \\ 1 & x = 1 \\ x^2 + 1 & x > 1 \end{cases}$$

a. $\lim_{x \rightarrow 1^-} f(x)$

b. $\lim_{x \rightarrow 1^+} f(x)$

c. $\lim_{x \rightarrow 1} f(x)$

