



### Understanding Limits Numerically and Graphically

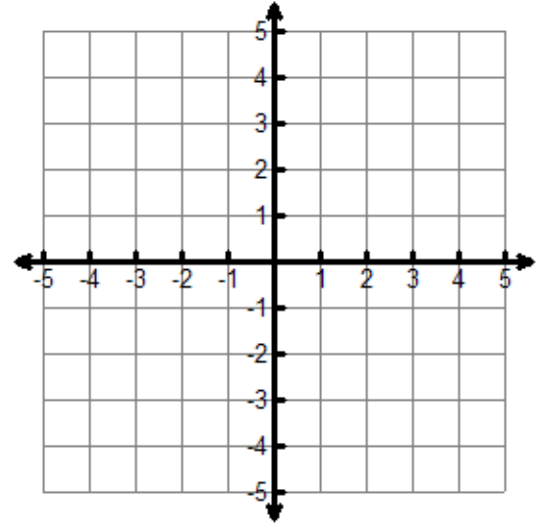
Use the given function to find the indicated limits, or state that the limit does not exist. Verify your answers graphically.

1.  $f(x) = \begin{cases} (x+2)^2 & \text{when } x < 0 \\ -\sqrt{x} + 4 & \text{when } x \geq 0 \end{cases}$

a.  $\lim_{x \rightarrow 0^-} f(x)$

b.  $\lim_{x \rightarrow 0^+} f(x)$

c.  $\lim_{x \rightarrow 0} f(x)$

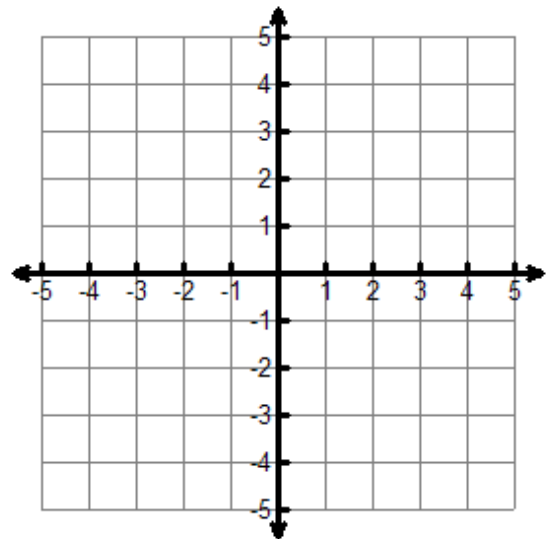


2.  $f(x) = \begin{cases} x^2 - 4 & x \leq 2 \\ x - 3 & x > 2 \end{cases}$

a.  $\lim_{x \rightarrow 2^-} f(x)$

b.  $\lim_{x \rightarrow 2^+} f(x)$

c.  $\lim_{x \rightarrow 2} f(x)$





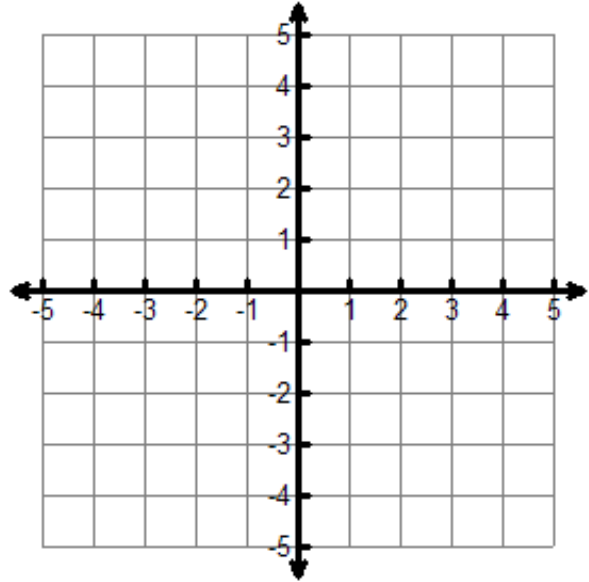
Understanding Limits Numerically and Graphically

$$3. f(x) = \begin{cases} -x & x < 1 \\ 1 & x = 1 \\ x^2 + 1 & x > 1 \end{cases}$$

a.  $\lim_{x \rightarrow 1^-} f(x)$

b.  $\lim_{x \rightarrow 1^+} f(x)$

c.  $\lim_{x \rightarrow 1} f(x)$

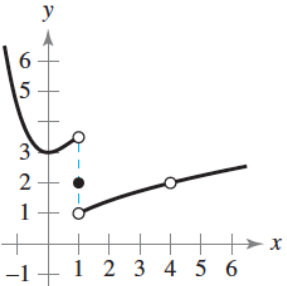


*Continued on Next Page...*

*There are no great limits to growth because there are no limits of human intelligence, imagination, and wonder.*

– Ronald Reagan

Answer the following questions. You may use a graphing calculator to assist you.

1	For the function $f(x) = 5x^2$ , as the $x$ -value gets closer and closer to 3, $f(x)$ gets closer and closer to what value?
2	For the function $f(x) = \frac{x^2 - 4}{x - 2}$ , as the $x$ -value gets closer and closer to 2, $f(x)$ gets closer and closer to what value?
3	For the function $f(x) = e^x + 1$ , as the $x$ -value gets closer and closer to 0, $f(x)$ gets closer and closer to what value?
<p>The graph of <math>f(x)</math> is given below, use the graph to answer the following questions.</p>  <p>4) a) <math>\lim_{x \rightarrow 4^-} f(x)</math>    b) <math>\lim_{x \rightarrow 4^+} f(x)</math>    c) <math>\lim_{x \rightarrow 4} f(x)</math>    d) <math>f(4)</math></p> <p>5) a) <math>\lim_{x \rightarrow 1^-} f(x)</math>    b) <math>\lim_{x \rightarrow 1^+} f(x)</math>    c) <math>\lim_{x \rightarrow 1} f(x)</math>    d) <math>f(1)</math></p>	
7	Simplify $\frac{x^2 + 7x + 12}{x^2 - 16}$